

ND - Normal duration, CD - crash duration  
 NC - Normal cost, CC - crash cost

Activity	ND	CD	NC	CC	Slope crash cost
A	120	100	12000	14000	\$ 100
B	20	15	1800	2800	\$ 200
C	40	30	16000	22000	\$ 600
D	30	20	1400	2000	\$ 60 ✓
E	50	40	3600	4800	\$ 120 ✓
F	60	45	13500	18000	\$ 300

To Determine Crash Cost Slope:

for activity A

$$S_A = \frac{CC - NC}{ND - CD}$$

→ slope for activity A

Activity A crash cost slope

Activity A Crash cost 1800/-

$$S_A = \frac{14000 - 12000}{120 - 100} = \frac{2000}{20}$$

$$S_A = 100 \text{ unit} \mid \$/day$$

Activity B

$$\frac{2800 - 1800}{20 - 15} = \frac{1000}{5} = \$200/day$$

Activity C

$$S_C = \frac{22000 - 16000}{40 - 30} = \frac{6000}{10} = \$600/day$$

Activity D

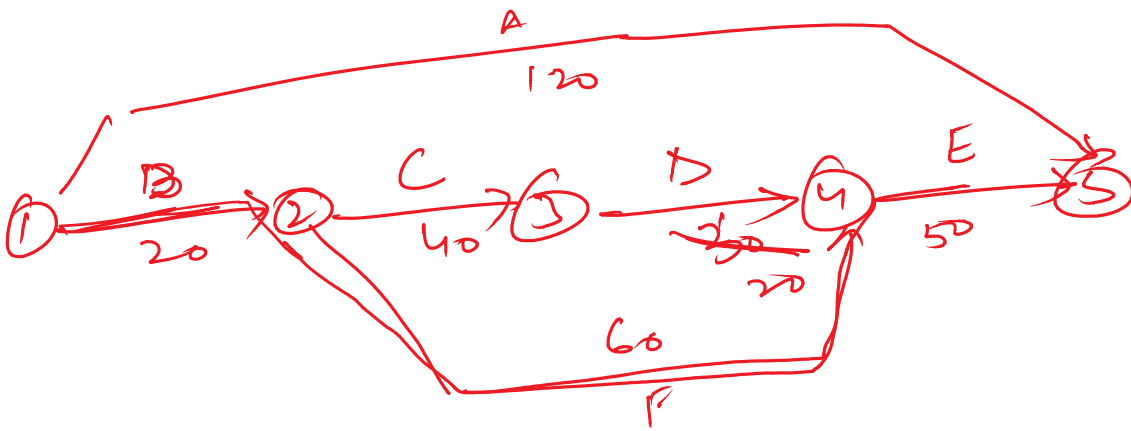
$$S_D = \frac{2000 - 1400}{30 - 20} = \$60/day$$

Activity E

$$S_E = \frac{4800 - 3600}{50 - 40} = \frac{1200}{10} = \$120/day$$

Activity F

$$S_F = \frac{18000 - 13500}{60 - 45} = \frac{4500}{15} = \$300/day$$



B - C - D - E = Normal duration  
 $20 + 40 + 30 + 50 = 140$  days.

Normal cost of project:

\$48300

overall duration will become 130 days

B - C - D - E = 130 days

B - F - E = 130 days.

Total project cost at 130 days

is Normal cost of the project + cost of crashing the activity D by 10 days

$$= \$48300 + 60 \times 10$$

$$= 48300 + \$600$$

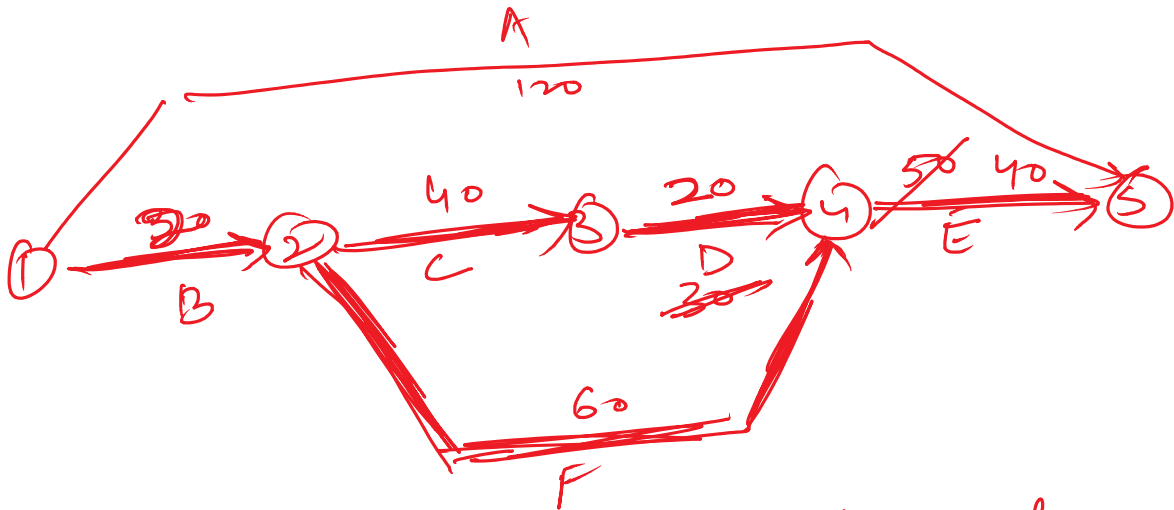
$$TC = \$48900$$

Next activity that would be crashed

is activity E

it has least slope crash cost of \$120/day

Activity E crashed by 10 days



Crashing for activity E by 10 days will cost additional \$120/day.

$$120 \times 10 = \$1200$$

Total duration = 120 days

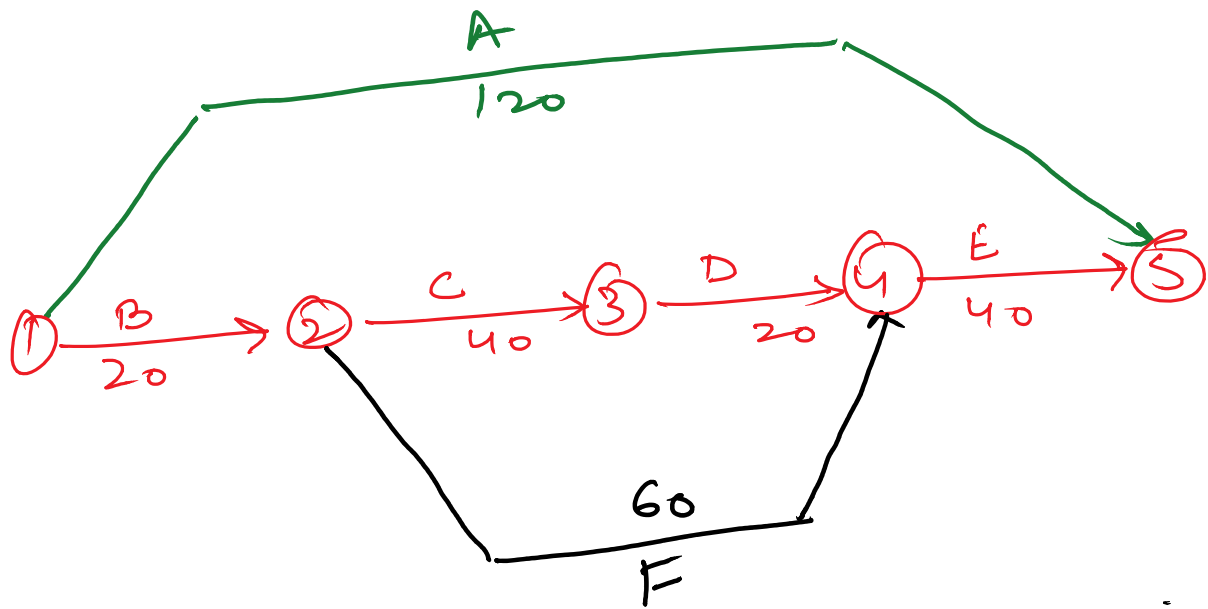
Total project cost = ~~50,100~~

$$= \$48,900 + \$1,200$$

$$= \$50,100$$

2 critical paths - those having zero float.

120 days to complete project.



Activity (A) is paired with each of the other activities to determine which has least slope crash cost for those activities which have remaining days to be crashed.

Activity A (\$100) + Activity B (\$200)

Activity A (\$100) + Activity C (\$600)

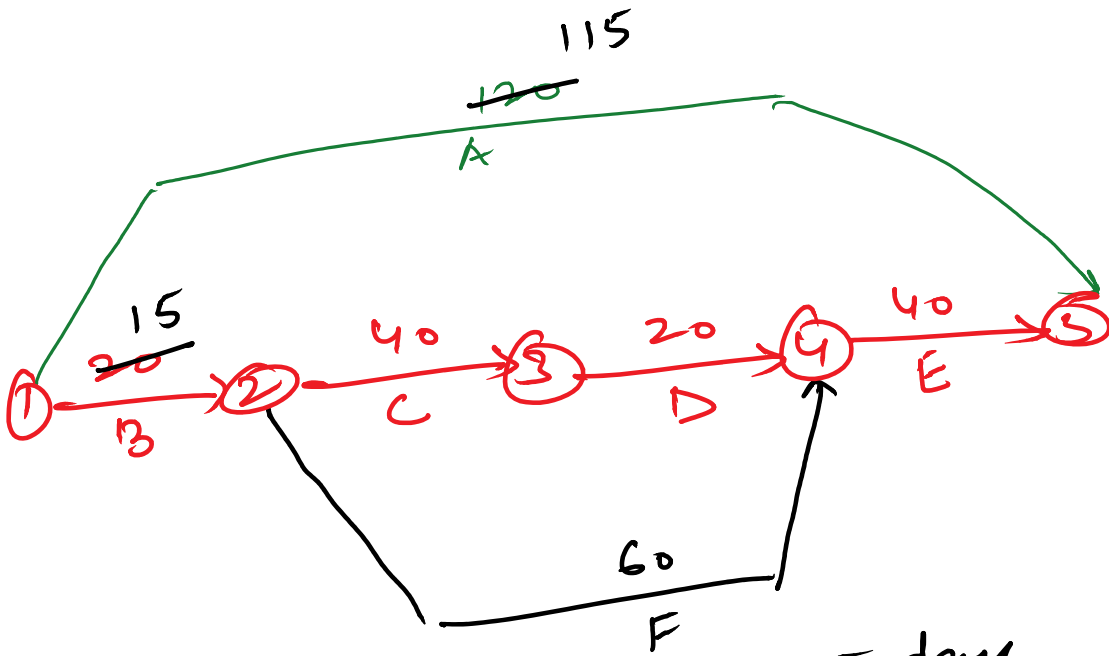
+ Activity F (\$300)

least crash cost slope

$$A (\$100) + B (\$200) = \$300/\text{day}$$

$$A (\$100) + C (\$600) + F (\$300)$$

$$= \$1000$$



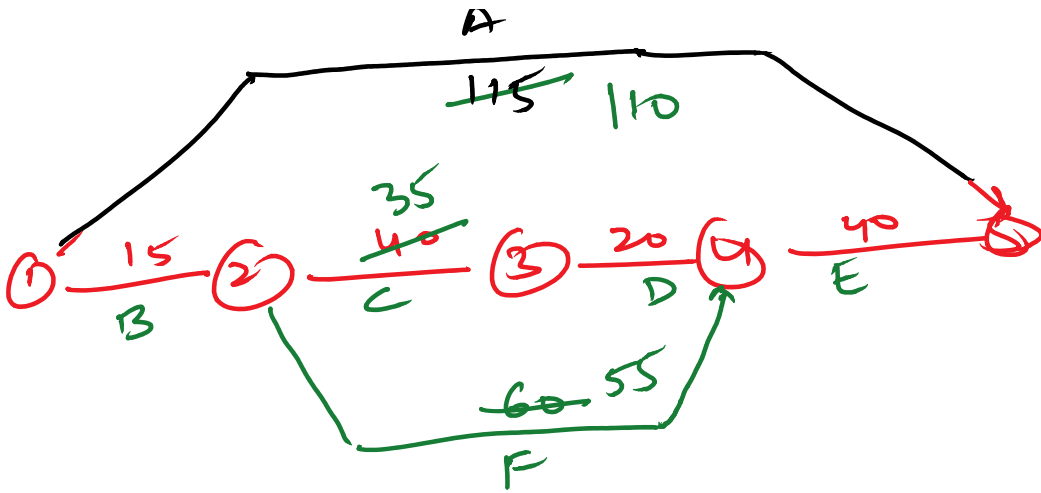
Reducing the project duration 5 days

$5 \times 300 = \$1500$  crashing cost &  
 the total cost will be:  $50100 + 1500$

Activity crashed here  $\Rightarrow$   $\$51600$   
 crashed anymore! & can't be

Total project duration is 110 days

A - C - F



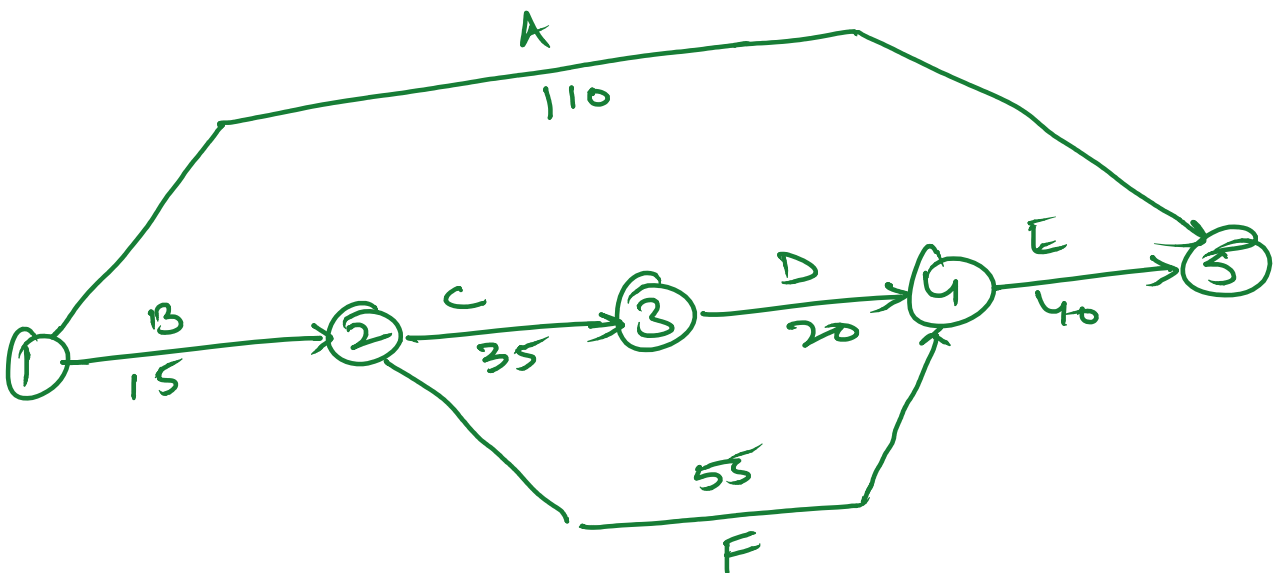
5 days for crashing — 110

$A + C + F$   
 $\$100 + \$180 + \$300 = \$1000$

$5 \text{ day} \times \$1000 = \$5000$

Total project duration will be = 110 days

Total project cost =  $51600 + 5000 = \$56600$



A — 110 days

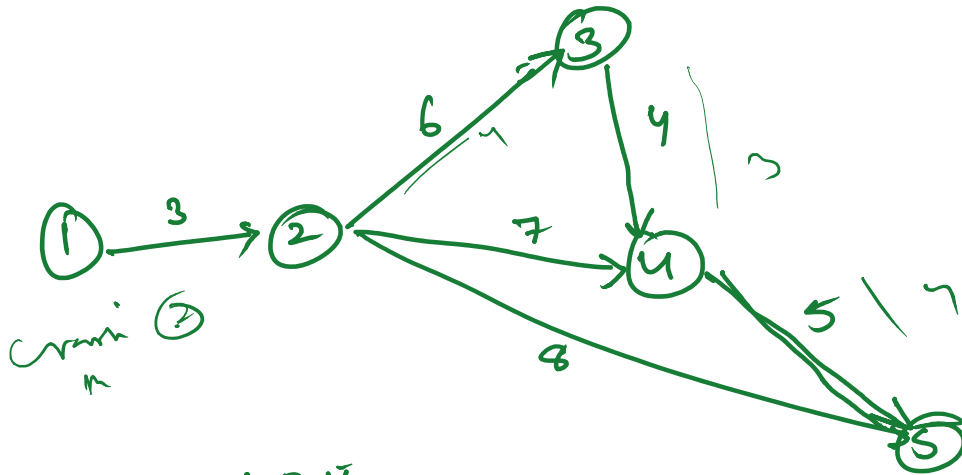
B - C - D - E = 110 days

B - F - E = 110 days

# Exercise 2

Construct a network diagram  
 Calculate project cost?  
 Indirect cost = ₹100/day

Activity	Normal		Crash	
	ND	NC	CD	CC
1-2	3	300	2	400
2-3	6	480	4	520
2-4	7	2100	5	2500
2-5	8	400	6	600
3-4	4	320	3	360
4-5	5	500	4	520



Crash path

$$1-2-3-4-5 = 18 \text{ days}$$

$$3 + 6 + 4 + 5 = 18 \text{ days (ND)}$$

$$2 + 4 + 3 + 4 = 13 \text{ days (Crash Duration)}$$

$$\text{Normal Cost} = 300 + 480 + 2100 + 400 + 320 + 500$$

$$= 4100$$

$$\text{Crash Cost} = 400 + 500 + 250 + 600 + 360 + 520 = 4900$$

Crash cost slope

Activity 1-2

$$= \frac{400 - 300}{3 - 2} = \frac{100}{1} = 100/\text{day}$$

Activity 2-3

$$\frac{520 - 480}{6 - 4} = \frac{40}{2} = 20/\text{day}$$

Activity 2-4

$$\frac{2500 - 2100}{7 - 5} = \frac{400}{2} = 200/\text{day}$$

Activity 2-5

$$\frac{600 - 400}{8 - 6} = \frac{200}{2} = 100/\text{day}$$

Activity 3-4

$$\frac{360 - 320}{4 - 3} = 40/\text{day}$$

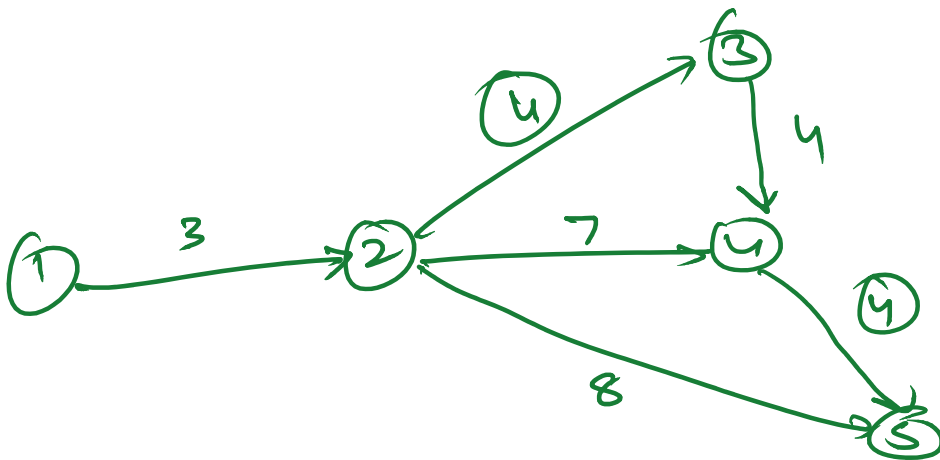
A . t . t . u . r

Activity 4-5

$$\frac{520 - 500}{5 - 4} = 20/\text{day}$$

Activity 2-3 & 4-5 have the least crash cost slope.

we will crash these 2 activities first.



from this network

after crashing, activity 2-3 is cut by 2 days & activity 4-5 is cut by 1 day

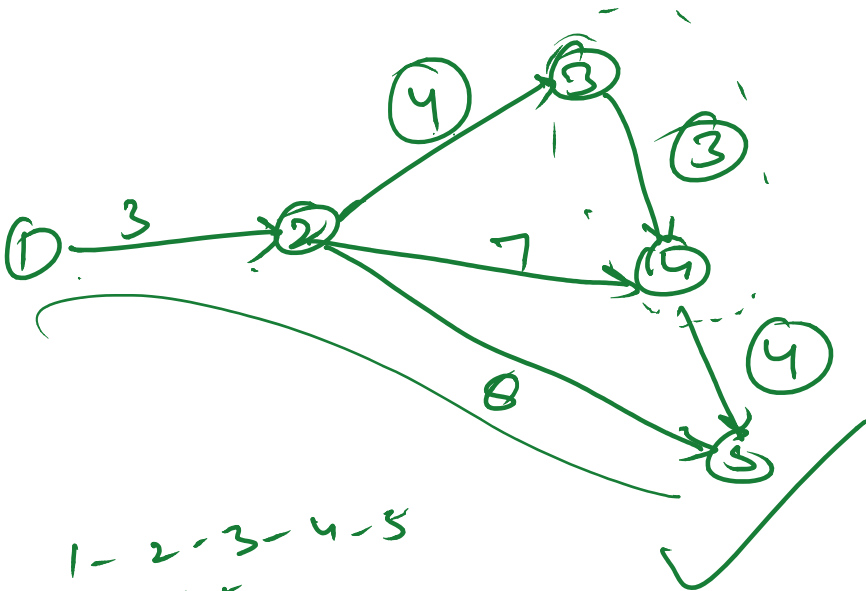
the critical path = 1-2-3-4-5

$$\text{the new project duration is} \\ = 3 + 4 + 4 + 4$$

= 15 days

~~cost~~ - ~~4000~~ ~~2000 + 2000~~

II<sup>nd</sup> stage. Activity 3-4



1-2-3-4-5  
14 days.

1-2-4-5 = 14 day

'there is no other activity on both the critical path which has cost slope less than indirect cost (100/-)

Optimum network -

∴ here a 14 days is the optimum project duration to complete the

project

$$\text{Total Indirect cost for 14 day} = 14 \times 100 = \underline{1400} -$$

Total project cost (optimum duration or path)

$$1-2, 2-3, 3-4, 4-5, 2-4, 2-5$$

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$$1-2, 2-3, 2-4, 2-5, 3-4, 4-5$$

$$\underline{300 + 520 + 2100 + 400 + 360 + 520}$$

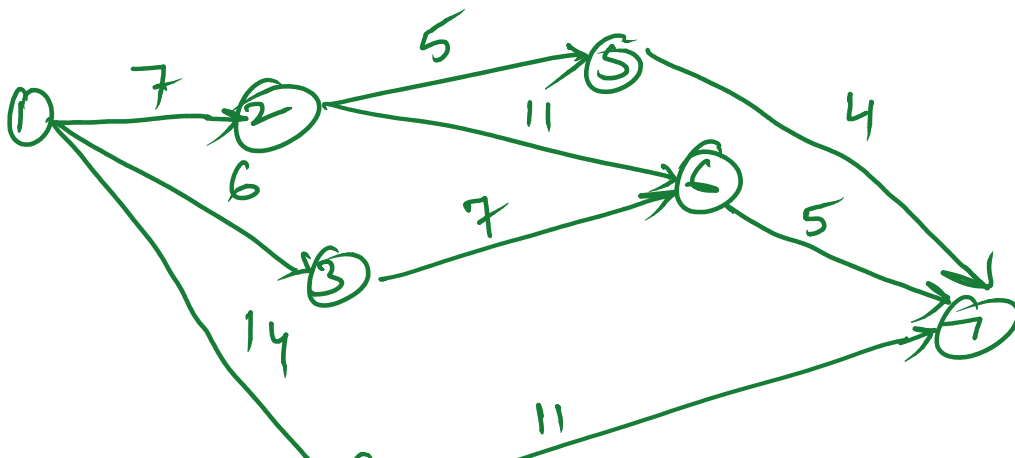
$$\approx 4200 + 1400 = \underline{5600} -$$

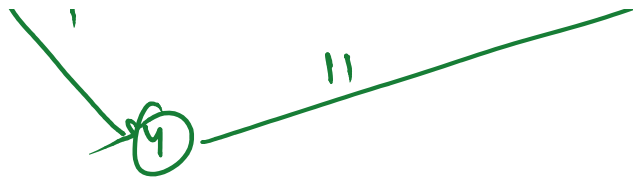
Normal duration = 18 days

$$TC = 4100 + 18 \times 100 = \underline{5900} -$$

Exercise 3

$$\text{Exp time} = \frac{t_0 + 4t_m + t_p}{6}$$





1-4-7 → 25 day

Project duration = 25 day.

Exercise 4

Activity	$t_o$	$t_p$	$t_m$	$t_e$	$\sigma^2$
1-2	3	15	6	7	4
1-3	2	14	5	6	4
✓ 1-4	6	30	12	14	16
2-5	2	8	5	5	1
2-6	5	17	11	11	4
3-6	3	15	6	7	4
✓ 4-7	3	27	9	11	16
5-7	1	7	4	4	1
6-7	2	8	5	5	1

$$t_e = \frac{t_o + t_p + 4 \times t_m}{6}$$

$$\sigma^2 = \left\{ \frac{t_p - t_o}{6} \right\}^2$$

$$\sigma^2 = \left\{ \frac{t_p - t_o}{6} \right\}$$

$$1 - 4 - 7 = 25 \text{ day}$$

$$t_o = 25 \text{ day}$$

We need to find the prob of project completed in 27 days?

$$\sigma = \sqrt{\sigma^2}$$

Sum of variances of critical path

$$1 - 4 - 7 = 16 + 16 = 32$$

$$\sigma = \sqrt{32}$$

$$\sigma = 5.65$$

$$Z = \frac{\mu - t_o}{\sigma}$$

path time

$$Z = \frac{27 - 25}{5.65}$$

$$= 0.35$$

from the Z table  
you we can get  
the value  
(3 - 0.35)



0.55

.6368  
63.689

