

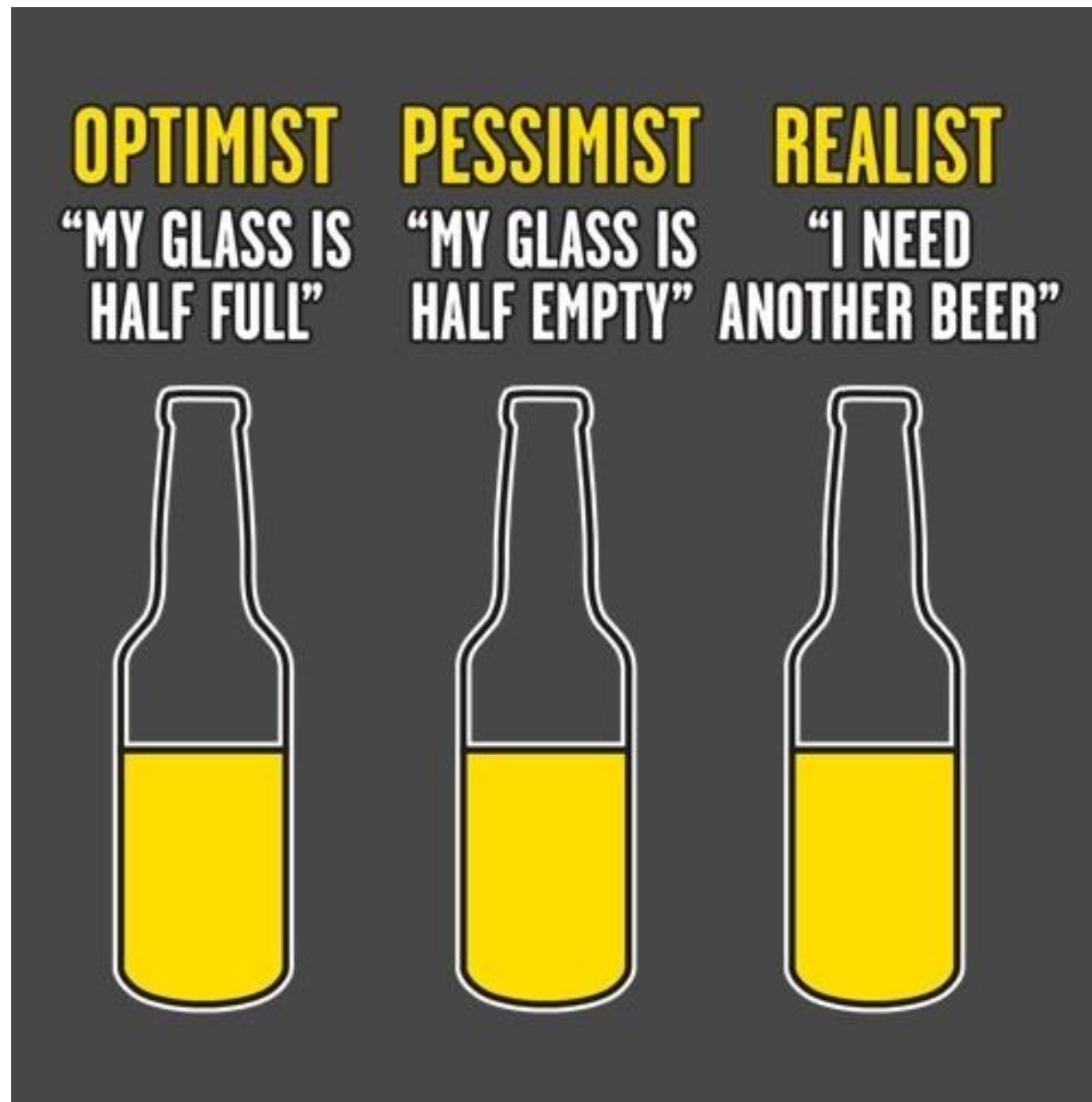
Decision Analysis

- ✓ A company owns a tract of land that may contain OIL
- ✓ One chance in four that land may contain OIL
- ✓ Revenue in case of finding oil is \$800,000. Drilling cost \$100,000.
- ✓ If land is sold revenue would be \$90,000

| <u>Alternatives</u> | <u>States of land</u> | |
|---------------------------------|------------------------------|---------------|
| | Oil | Dry |
| Drill for oil | \$700,000 | -\$100,000 |
| Sell the land | \$90,000 | \$90,000 |
| <u>Prior probability</u> | P(oil) = 0.25 | P(dry) = 0.75 |

Decisions; State of nature; Payoff table

- ✓ Optimist decision maker
- ✓ Pessimist decision maker
- ✓ Realist decision maker



Maximax pay-off criterion

- ✓ Ignore the probabilities
- ✓ Best of best payoffs

| <u>Alternatives</u> | <u>Status of land</u> | |
|---------------------|-----------------------|---------------|
| | Oil | Dry |
| Drill for oil | \$700,000 | -\$100,000 |
| Sell the land | \$90,000 | \$90,000 |
| | P(oil) = 0.25 | P(dry) = 0.75 |

The decision here would be??

Maximin pay-off criterion

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| <u>Alternatives</u> | <u>Status of land</u> | |
|---------------------|------------------------|------------------------|
| | Oil | Dry |
| Drill for oil | \$700,000 | -\$100,000 |
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| | $P(\text{oil}) = 0.25$ | $P(\text{dry}) = 0.75$ |

The decision here would be??

Maximum likelihood criterion

- ✓ Take into account the probabilities
- ✓ Best of pay-offs associated with higher probability

| <u>Alternatives</u> | <u>Status of land</u> | |
|---------------------|-----------------------|---------------|
| | Oil | Dry |
| Drill for oil | \$700,000 | -\$100,000 |
| Sell the land | \$90,000 | \$90,000 |
| | P(oil) = 0.25 | P(dry) = 0.75 |

The decision here would be??

Bayes Decision Rule

✓ Alternative that results in higher expected value

| <u>Alternatives</u> | <u>Status of land</u> | |
|---------------------|------------------------|------------------------|
| | Oil | Dry |
| Drill for oil | \$700,000 | -\$100,000 |
| Sell the land | \$90,000 | \$90,000 |
| | $P(\text{oil}) = 0.25$ | $P(\text{dry}) = 0.75$ |

The decision here would be??

- a) If the company is gasping to survive and can not afford to loose any money what soever. What decision rule should be employed?
- b) If the company is plush with abundant cash and can take any risk. What decision rule should be employed?
- c) Realistically speaking which decision rule should be adopted?

Sensitivity analysis

- ✓ Identify the range for probability for our decisions.
- ✓ Expected value from drilling = selling the land
- ✓ Crossover point.

| <u>Alternatives</u> | <u>Status of land</u> | |
|---------------------|-----------------------|-----------------------|
| | Oil | Dry |
| Drill for oil | \$700,000 | -\$100,000 |
| Sell the land | \$90,000 | \$90,000 |
| | $P(\text{oil}) = x$ | $P(\text{dry}) = 1-x$ |

| Alternatives | State of nature | | |
|---------------------|------------------------|-----|-----|
| | S1 | S2 | S3 |
| A1 | 220 | 170 | 110 |
| A2 | 200 | 180 | 150 |
| Prior probability | 0.6 | 0.3 | 0.1 |

1. Which alternative should be chosen under the maximax payoff criterion?
2. Which alternative should be chosen under the maximin payoff criterion?
3. Which alternative should be chosen under Bayes decision rule?
4. Which alternative should be chosen under maximum likelihood criterion.
5. Using Bayes decision rule, perform sensitivity analysis with respect to state S1 and S2 (without changing the prior probability of S3)